**EE475 HW#3 Fall 2019**

**Adaptive Linear Filtering**

We would like the filter to attenuate the noise, but at the same time not to blur the image details. Let’s do adaptive filtering to mitigate Gaussian noise in local neighborhood, centered at xy and of size nxn. Let be the local mean, be the signal variance in the neighborhood, the noise variance over all the image, f(x,y) the contaminated signal, g(x,y) the filtered signal. Consider the formula

If

Contaminate the Circuit-board image with zero-mean Gaussian noise having variance . Compare the image detail (e.g., legs of circuit components) preserving ability and noise removal performance of the following filters:

1. Filter the noisy image with 7x7 arithmetic mean filter
2. Filter it with the 7x7 geometric mean filter
3. Filter it with the above 7x7 adaptive linear filter
4. In general, you do not know the noise variance. How would you estimate it?

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**Adaptive Median Filter**

Median filter is effective in removing impulsive noise. But it collapses if the impulse noise density is above 20% and also for large windows can distort image details. Consider the following adaptive median filter that tries to remove salt-and-pepper noise, to smooth other types of noise and to reduce distortion on the image content. The standard median filter replaces every pixel with its median; this filter either does the median substitution or preserves the original value.

This filter has three goals: i) To remove salt-and-pepper noise; ii) smooth non-impulsive noise; iii) reduce image distortion and excessive thinning of image details.

Level A: “If zmin < zmed < zmax, go to B “ checks if zmed is a salt or pepper (impulse)

Level B: “If zmin < f(x,y) < zmax, output f(x,y)” checks if the center pixel itself is an impulse. If not, than either f(x,y) = zmin or f(x,y) = zmax; in either case, it is an impulse and must be smoothed with zmed.

zmin: minimum intensity value in the window

zmax: maximum intensity value in the window

zmed: median intensity value in the window

The algorithm is as follows:

A: If zmin < zmed < zmax, go to B

Else increase the window size

If window size ≤ max window size repeat A

Else, output zmed

B: If zmin < f(x,y) < zmax, output f(x,y)

Else output zmed

In the loop, start with 3x3 window and proceed till window size 7x7

1. Contaminate the Pentagon image with 25% salt and 25% pepper noise.
2. Filter the image with 7x7 median filter
3. Filter the image with the adaptive median filter where the loop starts with 3x3 window and proceeds till size 7x7
4. Compare and comment on the noise removal and image detail (e.g., cars in the carpark) preservation capability of the two filters



**Notch filtering**

The Moon and the Car images have been contaminated by a patterned interference.

1. Plot the spectrum of the image
2. Threshold the spectrum to identify the frequencies of the spectral peaks due to interference
3. Apply Gaussian notch filter to separate the interference pattern and the original image; plot them separately.

One can build a notch filter, i.e., a band-stop filter by starting with a low-pass filter

HLP(u,v): HHP(u,v) = 1 - HLP(u,v). For example, ideal HP filter

, where is the parameter to adjust the bandwidth

and D(u,v) is the Euclidean distance from the center of MxN rectangle, i.e.,

. The Gaussian high-pass filter then has the form .

The notch filter is simply where Q is the number of observed peak pairs , and . In this expression, , and denote the notch filter pair at frequencies .

Note that the product operation is over frequency transfer functions. Since you are going to implement the filtering with frequency masks (matrices), you should interpret this operation as successive applications of the filtering operation for k = 1, …, Q.

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**Heat Maps**

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Consider the Rose image. Contaminate it with salt-and-pepper noise with increments of 3%, from 3% to 30%. Try to remove the noise with a median filter with window sizes 3x3, 5x5, 7x7, 9x9, 11x11, 13x13. To show the improvements, if any, brought in by the median filter plot the image quality index SSIM before and after median filtering as a function of window size using a heat map.

**Note 1:**

In scientific research, we are often confronted with the problem of presenting a large quantity of numerical results, e.g., thousands of numbers. Just listing the numbers is not the best approach. Heat map is a visualization tool that at one look will tell the essence of all that bunch of numbers (http://en.wikipedia.org/wiki/Heat\_map).

Plot the noise intensity, i.e., salt-and-pepper percentage on the horizontal axis and the filter size on the vertical axis. For the heatmap, you can use matlab's imagesc, colormap and colorbar functions. The heat should be proportional to the performance; in our case, the lower the S&P percentage, the better it is. Set blue to good performance, red to poor performance. For example, use colormap(flipud(jet)).

**Note 2:**

There are several metrics to measure image quality and the performance of image processing algorithms. The most common one is the Peak-Signal-to-Noise-Ratio where J and I are, respectively, the processed and the input images. SNR or PSNR is criticized for not reflecting subjective evaluations. Also PSNR needs a reference image. Another index, more reflective of human judgement and also one that does not need a reference image is SSIM: Structural Similarity Index Measure:

<https://en.wikipedia.org/wiki/Structural_similarity>

<https://www.mathworks.com/help/images/image-quality-metrics.html?requestedDomain=www.mathworks.com>